PURCHASING POWER PARITY

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Review: Arbitrage

• Last Class, we reviewed the impact of arbitrage on FX Markets.

Arbitrage requires three elements: Pricing mistakes, no risk, & no own capital –that is, borrowing is needed.

We went over three forms of arbitrage:

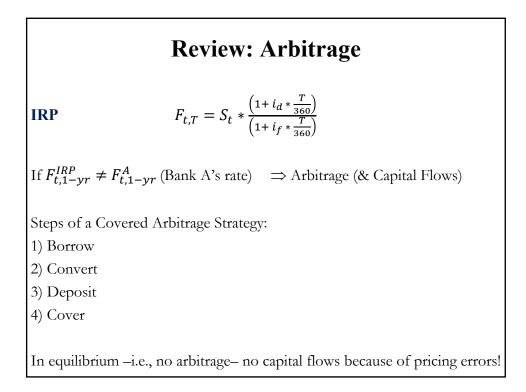
Local (sets uniform rates across banks)

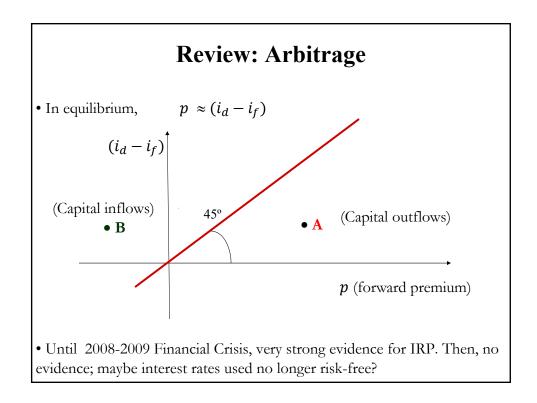
Triangular (sets cross rates)

Covered (sets forward rates)

From covered arbitrage, we derived a formula for $F_{t,T}$:

$$F_{t,T} = S_t * \frac{\left(1 + i_d * \frac{T}{360}\right)}{\left(1 + i_f * \frac{T}{360}\right)}$$
(Interest Rate Parity Theorem





Review: Theories of FX Determination

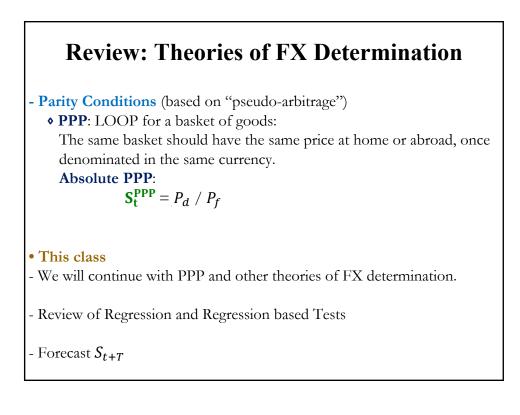
• Theories of FX rates determination:

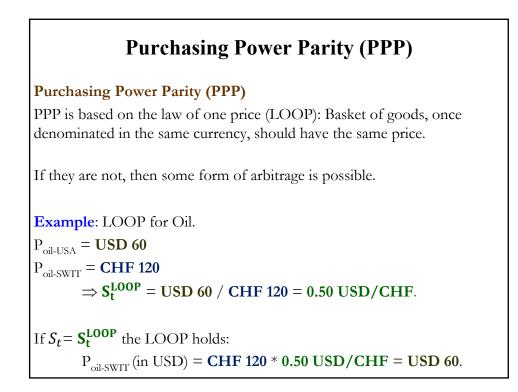
- PPP (based on Price and Inflation rates differentials)
- IFE (based on interest rates differentials)
- EH (based on uncovered IRP -i.e., no covered step)
- Macroeconomic Models

♦ RW

• <u>Goal 1</u>: Explain S_t with a theory, say T1. Then, $S_t^{T1} = f(.)$

• <u>Goal 2</u>: Eventually, produce a formula to forecast S_{t+T} $S_{t+T} = f(X_t) \implies \mathbb{E}[S_{t+T}]$





Example (continuation):Suppose $S_t = 0.75$ USD/CHF \Rightarrow Oil in Switzerland is more expensive (inUSD) than in the US: $P_{oil-SWTT}$ (USD) = CHF 120 * 0.75 USD/CHF = USD 90 > $P_{oil-USA}$ \Rightarrow LOOP is not holdingTrading strategy:(1) Buy oil in the US at $P_{oil-USA} = USD 60$.(2) Export oil to Switzerland.(3) Sell US oil in Switzerland at $P_{oil-SWTT} = CHF 120$.(4) Sell CHF/buy USD at then S_t .Strategy, exporting US of oil to Switzerland, will affect prices:1) $P_{oil-USA}^{\uparrow}$ 2) $P_{oil-USA}^{\uparrow}$ 2) $P_{oil-USA}^{\uparrow}$ 3) $S_t \downarrow$ S_t^{LOOP} \uparrow (= $P_{oil-USA}^{\uparrow}/P_{oil-SWTT}^{\downarrow}$)3) $S_t \downarrow$ $S_t \Leftrightarrow S_t^{LOOP}$ (convergence). ¶

Example (continuation):

LOOP Notes :

 LOOP gives an equilibrium exchange rate.
 Equilibrium is achieved when there is no trade in oil (because of pricing mistakes): LOOP holds for oil!



• LOOP is telling what S_t should be (in equilibrium). Not what S_t is in the market today.

• Using the LOOP we have generated a model for S_t . When applied to many goods, we have the **PPP model**.

Absolute version of PPP: The FX rate between two currencies is the ratio of the two countries' general price levels:

 S_t^{PPP} = Domestic Price level / Foreign Price level = P_d/P_f

Example: LOOP for CPIs. CPI-basket_{USA} = P_{USA} = USD 5,577 CPI-basket_{SWTT} = P_{SWTT} = CHF 6,708 $\Rightarrow S_t^{PPP}$ = USD 5,577/CHF 6,708 = 0.8314 USD/CHF. If $S_t \neq 0.8314$ USD/CHF, there will be trade of the goods in the baskets. Suppose S_t = 1.09 USD/CHF > S_t^{PPP} . Then, P_{SWTT} (in USD) = CHF 6,708 * 1.09 USD/CHF = USD 7,311.72 > P_{USA} = USD 5,577 Example (continuation): (disequilibrium: $S_t = 1.09 \text{ USD/CHF} > S_t^{PPP}$) P_{SWTT} (in USD) = CHF 6,708 * 1.09 USD/CHF $= \text{USD 7,311.72} > P_{USA} = \text{USD 5,577}$ Potential profit: USD 7,311.72 – USD 5,577 = USD 1,734.72 Traders will do the following *pseudo-arbitrage* strategy: 1) Borrow USD 2) Buy the CPI-basket in the U.S. 3) Sell the CPI-basket, purchased in the U.S., in Switzerland. 4) Sell the CHF/Buy USD 5) Repay the USD loan, keep the profits. Note: "Equilibrium forces" at work: $\begin{pmatrix} 2 \end{pmatrix} P_{USA} \uparrow \\ & 3 \end{pmatrix} P_{SWTT} \downarrow \qquad (\Rightarrow S_t^{PPP} \uparrow = P_{USA} \uparrow / P_{SWTT} \downarrow)$ $4) S_t \downarrow \qquad S_t \Leftrightarrow S_t^{PPP}$ (converge) ¶

• Real v. Nominal Exchange Rates

The absolute version of the PPP theory is expressed in terms of S_t , the *nominal exchange rate*.

We can write the absolute version of the PPP relationship in terms of the *real exchange rate*, R_r . That is,

$$\mathbf{R}_{t} = \mathbf{S}_{t} P_{f} / P_{d} = 1$$

R_t allows us to compare prices, translated to DC:

If $\mathbf{R}_{t} > 1$, foreign prices (translated to DC) are more expensive

If $\mathbf{R}_{t} = 1$, prices are equal in both countries –i.e., PPP holds!

If $\mathbf{R}_{t} < 1$, foreign prices are cheaper

Economists associate $\mathbf{R}_{t} > 1$ with a more efficient domestic economy.

Example: Using the Big Mac prices in Switzerland & the US: $P_f = CHF 7.10$ $P_d = USD 5.69$ $S_t = 1.1497 USD/CHF$ $\Rightarrow P_f$ (in USD) = USD 8.16 > P_d $R_t = S_t P_{SWIT}/P_{US} = 1.14925 * CHF 7.10/USD 5.69 = 1.4345$ Taking the Big Mac as our basket, the U.S. is more competitive thanSwitzerland. Swiss prices are 43.45% higher than U.S. prices, after takinginto account the nominal exchange rate.To bring the economy to equilibrium –no trade in Big Macs-, we expect theUSD to appreciate against the CHF. \Rightarrow Trading Signal: Buy USD/Sell CHF. ¶

• The Big Mac ("Burgernomics," popularized by *The Economist*) has become a popular basket for PPP calculations. Why?

1) Standardized, common basket: beef, cheese, onion, lettuce, bread, pickles and special sauce. (CPI baskets, not standardized). Sold in 120+ countries.

Big Mac (Sydney)



Big Mac (Tokyo)

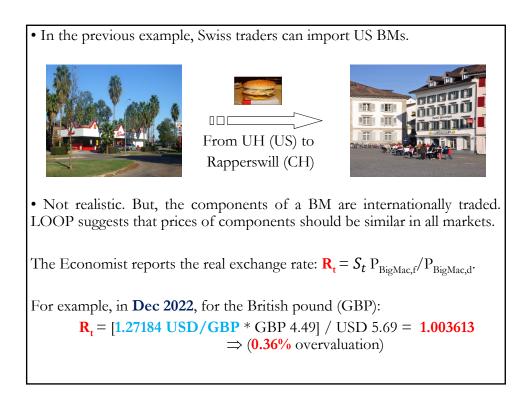


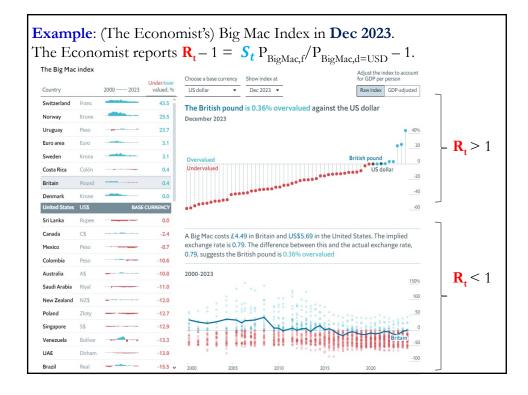
2) Very easy to find out the price.

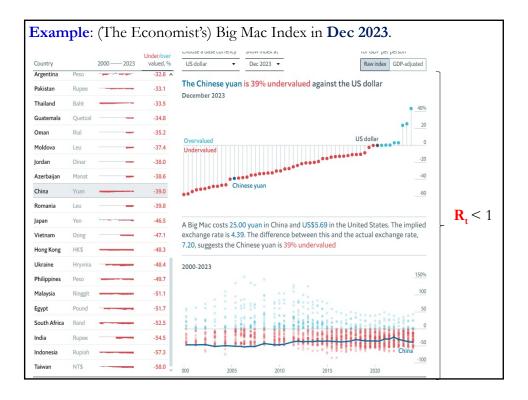
3) It turns out, it is correlated with more complicated common baskets.

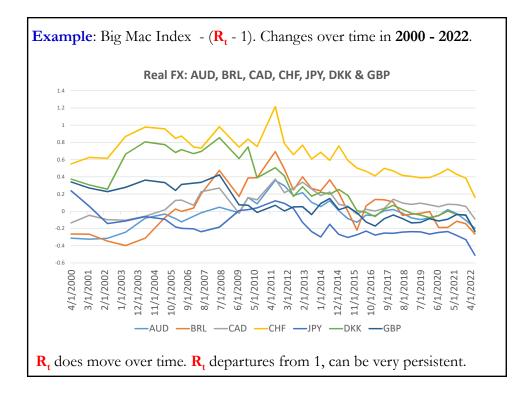
• In theory, traders can exploit the price differentials in BMs.

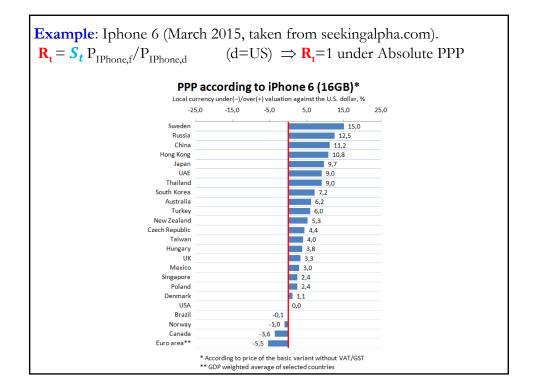
<u>The Economist's Big Mac Index</u>











• Empirical Evidence: Simple informal test: Test: If Absolute PPP holds \Rightarrow **R**_t = 1. In the Big Mac example, PPP does not hold for the majority of countries. \Rightarrow Absolute PPP, in general, fails (especially, in the short-run). <u>Absolute PPP: Qualifications</u> (1) PPP emphasizes only trade and price levels. Political/social factors, financial problems, etc. are ignored. (2) Implicit assumption: Absence of trade frictions (tariffs, quotas, taxes, etc.). Not Realistic. One of the big criticism. 3) PPP is unlikely to hold if P_f and P_d represent *different baskets*. This is why the Big Mac is a popular choice. (4) Trade takes time (contracts, information problems, etc.). (5) Internationally non-traded/non-tradable (NT) goods -i.e. haircuts, home and car repairs, medical services, real estate. The NT good sector is big: 50%-60% of consumption (big weight in CPI basket).

• Absolute PPP: Qualifications - No trade frictions?

Even before the Trump tariffs, many everyday goods were protected in the U.S.:

- Peanuts (shelled 131.8%, and unshelled 163.8%).

- Paper Clips (as high as 126.94%)

- European Roquefort Cheese, cured ham, mineral water (100%)
- Japanese leather (40%)
- Sneakers (48% on certain sneakers)

- Chinese tires (35%)

- Canned Tuna (as high as **35%**)
- Synthetic fabrics (32%)
- Steel (25%)
- Indian wood furniture (25%)
- Italian footwear & eyeglasses (25%)
- Brooms (quotas and/or tariff of up to 32%)
- Trucks (25%) & cars (2.5%)

• Absolute PPP: Qualifications - No trade frictions?

Some Japanese protected goods:

- Rice (**778%**)
- Sugar (**328%**)
- Powdered Milk (218%)
- Beef (38.5%, but can jump to 50% depending on volume).

Some European protected goods:

- Knitted Clothes (100%)
- Fresh Cheese (48.3%)
- Bovine Meat, boneless (41%)
- Fresh or dried grapefruit (25%)
- Atlantic Salmon (25%)

• Absolute PPP: Qualifications - NT Sector & Borders

The NT sector also has an effect on the price of traded goods. For example, rent and utilities costs affect the price of a Big Mac: 25% of Big Mac due to NT goods.

• Empirical Fact

Price levels in richer countries are consistently higher than in poorer ones. This fact is called the *Penn effect*. Many explanations, the most popular: The **Balassa-Samuelson (BS) effect**.

Borders Matter

You may look at the Big Mac Index and think: "No big deal: there is also a big dispersion in prices within the U.S., within Texas, and, even, within Houston!"

True. Prices vary within the U.S. For example, in **2015**, the price of a Big Mac (and Big Mac Meal) in New York was USD 5.23 (USD 7.45), in Texas as USD 4.39 (USD 6.26).

But, borders play a role, not just distance!

Engel and Rogers (1996) computed the variance of LOOP deviations for **city pairs** within the **U.S.**, within **Canada**, and **across the border**.

<u>Conclusion</u>: Distance between cities within a country matter, but the **border effect** is **significant**.

To explain the difference between prices across the border using the estimate distance effects within a country, they estimate the U.S.-Canada border should have a width of **75,000 miles**!

This huge estimate has been revised downward, but a large positive border effect remains.

Balassa-Samuelson Effect
Labor costs affect all prices. We expect average prices to be cheaper in poor countries than in rich ones because labor costs are lower.
This is the Balassa-Samuelson effect: Rich countries have higher productivity and, thus, higher wages in the traded-goods sector than poor countries do. But, firms compete for workers.
Then, wages in NT goods and services are also higher

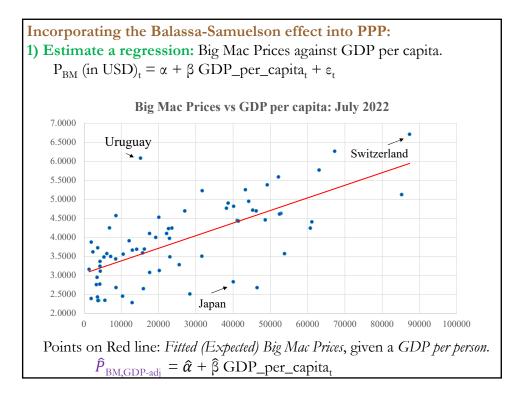
 \Rightarrow Overall prices are lower in poor countries.

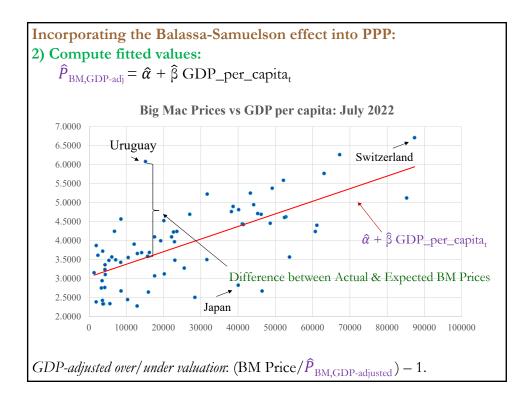
• For example, in **2000**, a typical McDonald's worker in the U.S. made **USD 6.50/hour**, while in China made **USD 0.42/hour**.

In 2021, the same numbers for a cashier are USD 10/hour and USD 1.76.



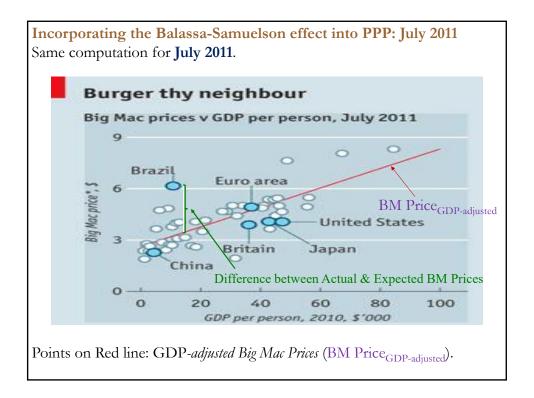
• Balassa-Samuelson effect: A positive correlation between *PPP exchange rates (overvaluation)* and high productivity countries.

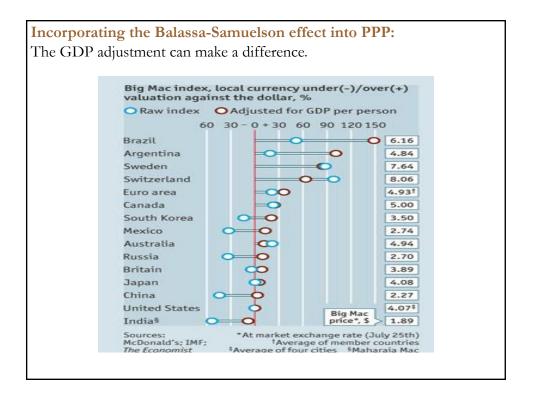




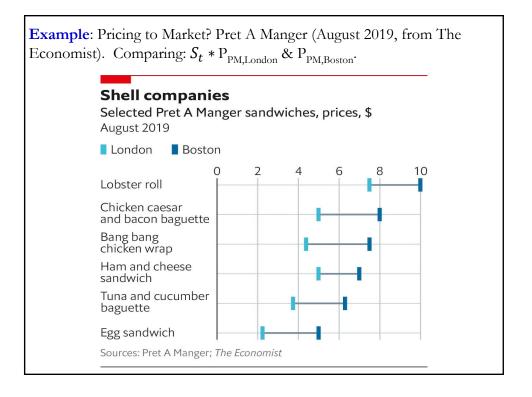
Incorporating the Balassa-Samuelson effect into PPP: Computations Using data from The Economist for July 2022, we estimate the red line: $\hat{P}_{BM,GDP-adj} = 3.045895 + 0.0000332 * GDP_per_capita_t$ Now, we can compute the "**Expected BM prices**, given the GDP of a given country." **Example**: Uruguay calculations. Uruguay's GDP per capita in July 2022 was **USD 15,169.153**. Then, $\hat{P}_{BM,GDP-adj}$ (Uruguay) = 3.045895 + 0.0000332 * **15,169.153** = **3.549511** That is, the expected BM in Uruguay in July 2022, given its GDP per capita, was **USD 3.55**. Since the observed local BM price was **UYU 255**, which translates to **USD 6.08** (= **UYU 255/41.91 UYU/USD**), then the *GDP-adjusted over/under valuation* was: **6.08 / 3.549511** - 1 = 71.29% (71.29% overvalued)

• Empirical Evidence: Simple informal test: Test: If Absolute PPP holds \Rightarrow **R**_t = 1. In the Big Mac example, PPP does not hold for the majority of countries. \Rightarrow Absolute PPP, in general, fails (especially, in the short-run). • Absolute PPP: Qualifications (1) PPP emphasizes only trade and price levels. Political/social factors, financial problems, etc. are ignored. (2) Implicit assumption: Absence of trade frictions (tariffs, quotas, taxes, etc.). Not Realistic. One of the big criticism. 3) PPP is unlikely to hold if P_f and P_d represent *different baskets*. This is why the Big Mac is a popular choice. (4) Trade takes time (contracts, information problems, etc.). (5) Internationally non-traded/non-tradable (NT) goods -i.e. haircuts, home and car repairs, medical services, real estate. The NT good sector is big: 50%-60% of consumption (big weight in CPI basket).





Pricing-to-Market Krugman (1987): Positive relationship between GDP and price levels is caused by Pricing-to-market –i.e., price discrimination.
Producers discriminate: Same good is sold to rich countries at higher prices than to poorer countries.
Alessandria and Kaboski (2008): U.S. exporters, on average, charge the richest country a 48% higher price than the poorest country.
But pricing-to-market struggles to explain why PPP does not hold among developed countries with similar incomes.
For example, Baxter and Landry (2012) report that IKEA prices deviate 16% from the LOOP in Canada, but only 1% in the U.S.



Main PPP criticism

Absolute PPP does not incorporate transaction costs and frictions. Relative PPP allows for fixed transaction costs/frictions (say, a fixed USD amount).

Relative PPP

The rate of change in the prices of products should be similar when measured in a common currency (as long as trade frictions are unchanged):

$$e_{f,t,T}^{\text{PPP}} = \frac{S_{t+T}^{PPP} - S_t}{S_t} = \frac{(1 + I_d)}{(1 + I_f)} - 1 \quad (\text{Relative PPP})$$

where,

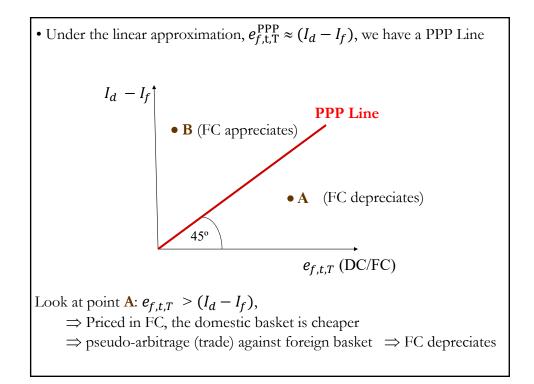
 I_f = foreign inflation rate from t to t + T.

 I_d = domestic inflation rate from t to t + T.

Note: $e_{f,t,T}^{PPP}$ is an expectation; what we expect to happen in equilibrium from t to t + T.

• Linear approximation: $e_{f,t,T}^{PPP} \approx (I_d - I_f) \implies$ one-to-one relation

Relative PPP • Linear approximation: $e_{f,t,T}^{PPP} \approx (I_d - I_f) \implies$ one-to-one relation **Example:** From t = 0 to t + T = 1, prices increase 10% in Mexico relative to prices in Switzerland. Then, S_t should also increase 10%. If $S_{t=0} = 9 \text{ MXN/CHF}$ $\Rightarrow S_{t=1}^{PPP} = E[S_{t=1}] = 9 \text{ MXN/CHF} * (1 + .10) = 9.9 \text{ MXN/CHF}$ Suppose at t = 1, S_t increases 13.33%. Then, $S_{t=1} = 10.2 \text{ MXN/CHF} > S_{t=1}^{PPP} = 9.9 \text{ MXN/CHF}$ \Rightarrow According to Relative PPP, the CHF is overvalued. ¶ Notation: $E[S_{t=1}] = \text{Expected value of } S_{t=1} \pmod{3}$, a predicted value. Example: Forecasting S_t (USD/ZAR) using PPP (ZAR=South Africa). It is Dec 2024. You have the following information: $CPI_{US,2024} = 104.5$, $CPI_{SA,2024} = 100.0$, $S_{t=2024} = .2035$ USD/ZAR. You are given the 2025 CPI's forecast for the U.S. and SA: $E[CPI_{US,2025}] = 110.8$ $E[CPI_{SA,2025}] = 102.5$. You want to forecast S_{2025} using the relative (linearized) version of PPP. $E[I_{US,2025}] = (110.8/104.5) - 1 = .06029$ $E[I_{SA,2025}] = (102.5/100) - 1 = .025$ $E[S_{2025}] = S_{2024} * (1 + e_{f,t=2024,T=2025}^{PPP}) = S_{2024} * (1 + E[I_{US}] - E[I_{SA}])$ = .2035 USD/ZAR * (1 + .06029 - .025) = .2107 USD/ZAR.



<u>Relative PPP: Implications</u>

(1) Under relative PPP, \mathbf{R}_{t} remains constant (it can be different from 1!).

(2) Without relative price changes, an MNC faces no real operating FX risk (as long as the firm avoids fixed contracts denominated in FC).

• Relative PPP: Absolute versus Relative

- Absolute PPP compares price levels.

Under Absolute PPP, prices are equalized across countries:

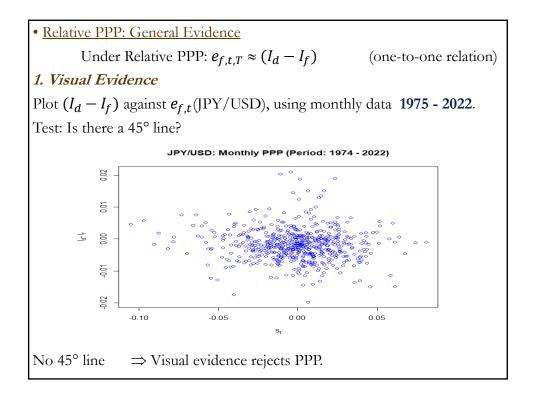
"A mattress costs **GBP 200** (= **USD 320**) in the U.K. and **BRL 800** (= **USD 320**) in Brazil."

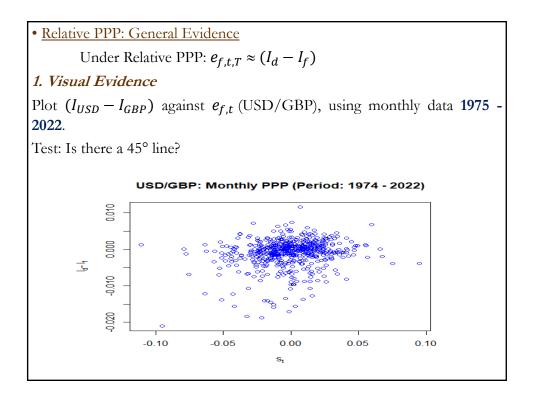
- Relative PPP compares price changes.

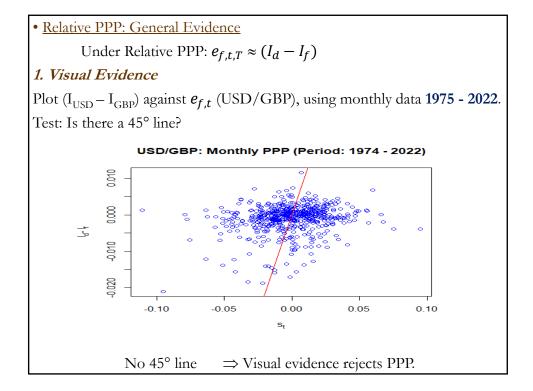
Under Relative PPP, exchange rates change by the same amount as the inflation rate differential (original prices can be different):

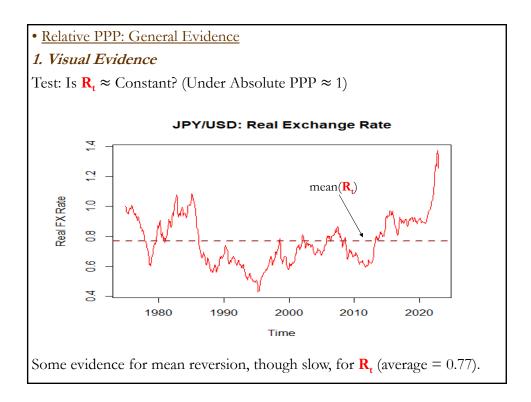
"U.K. inflation was 2% while Brazilian inflation was 8%. Meanwhile, the BRL depreciated 6% against the GBP. Then, relative cost comparison remains the same."

• Relative PPP is weaker than Absolute PPP: \mathbf{R}_{t} can be different from 1. • <u>Relative PPP: Testing</u> <u>Key</u>: On average, what we expect to happen, $e_{f,t,T}^{PPP}$, should happen, $e_{f,t,T}$. \Rightarrow On average: $e_{f,t,T} \stackrel{?}{\approx} e_{f,t,T}^{PPP} \approx (I_d - I_f)$ or $\mathbf{E}[e_{f,t,T}] \stackrel{?}{\approx} \mathbf{E}[e_{f,t,T}^{PPP}] \approx \mathbf{E}[(I_d - I_f)]$ We use a linear regression to test relative PPP: We regress $e_{f,t}$ on $(I_d - I_f)$: $e_{f,t,T} = \frac{S_{t+T} - S_t}{S_t} = \alpha + \beta (I_d - I_f)_{t+T} + \varepsilon_{t+T}$, where ε_t : regression error. That is, $\mathbf{E}[\varepsilon_{t+T}] = 0$. Then, $\mathbf{E}[e_{f,t,T}] = \alpha + \beta \mathbf{E}[(I_d - I_f)_{t+T}] + \mathbf{E}[\varepsilon_{t+T}] = \alpha + \beta \mathbf{E}[e_{f,t,T}^{PPP}]$ $\Rightarrow \mathbf{E}[e_{f,t,T}] = \alpha + \beta \mathbf{E}[e_{f,t,T}^{PPP}]$









• <u>Relative PPP: General Evidence</u> (continuation)

In the long run, \mathbf{R}_t moves around some mean number (long-run PPP parity?). But, the deviations from long-run parity are very **persistent**.

Economists report the number of years that a PPP deviation is expected to decay by 50%, the **half-life**. The half-life is in the range of **3 to 5 years** for developed currencies. Very slow!

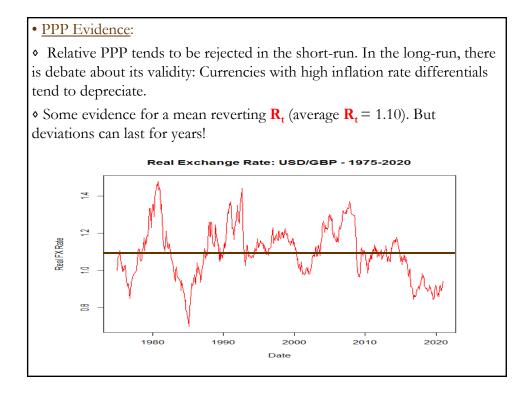
	I _{JPY}	I _{USD}	$I_{JPY} - I_{USD}$	$e_{\mathrm{f,t,T}\mathrm{(JPY/USD)}}$
Mean	0.00125	0.00303	-0.00179	-0.00139
SD	0.00485	0.00322	0.00502	0.02622
Min	-0.01095	-0.01786	-0.01981	-0.08065
Median	0.00102	0.00266	-0.00184	0.00022
Max	0.02558	0.01420	0.02104	0.08066

I and mun on average

2. Statistical Evidence Formal test: Regression $e_{f,t,T} = \alpha + \beta (I_d - I_f)_{t+T} + \varepsilon_{t+T}, \quad (\varepsilon_t: \text{ error term, E}[\varepsilon_t] = 0).$ The null hypothesis is: H_0 (Relative PPP true): $\alpha = 0$ and $\beta = 1$ H_1 (Relative PPP not true): $\alpha \neq 0$ and/or $\beta \neq 1$ • <u>Tests</u>: *t-test* (individual tests on α and β) & *F-test* (joint test) (1) Individual test: *t-test* $t-test = t_0 = [\hat{\theta} - \theta_0]/S.E.(\hat{\theta})$ where θ represents α or $\beta \implies (\theta_0 = \alpha \text{ or } \beta \text{ evaluated under } H_0).$ Statistical distribution: $t_0 \sim t_v$ (v = N - K = degrees of freedom) K = # parameters in model, & N = # of observations. <u>Rule</u>: If $|t-test| > |t_{v,1-\alpha/2}|$, reject H_0 at the α level. When v = N - K > 30, $t_{30+,975} \approx 1.96 \implies 2\text{-sided C.I. } \alpha = .05$ (5 %) 2. Statistical Evidence (2) Joint Test: *F-test* $F = \frac{[RSS(H_0) - RSS(H_1)]/J}{RSS(H_1)/(N-K)}$ Statistical distribution: $F \sim F_{J,N-K,\alpha}$ J = # of restrictions in H_0 (under PPP, $J=2: \alpha=0 \& \beta=1$) K = # parameters in model (under PPP model, $K=2: \alpha \& \beta$) N = # of observations RSS = Residuals Sum of Squared, $\hat{\varepsilon}_t = error_t = e_{f,t} - [\hat{\alpha} + \hat{\beta} (I_{d,t} - I_{f,t})]$. $RSS(H_0) = \sum_{t=1}^{N} [e_{f,t} - (I_{d,t} - I_{f,t})]^2$ $RSS(H_1) = \sum_{t=1}^{N} (\hat{\varepsilon}_t)^2$ <u>Rule</u>: If $F > F_{J,N-K,1-\alpha}$ reject at the α level. Usually, $\alpha = .05$ (5 %) When N > 300, $F_{J=2,300+,\alpha=.95} \approx 3$.

Example: Using monthly Japanese and U.S. data (1975: Jan - 2022: Dec), we fit the following regression (Observations = 576): $e_{f,t,T}(\text{JPY/USD}) = (S_t - S_{t-1})/S_{t-1} = \alpha + \beta (I_{IAP} - I_{US})_t + \varepsilon_t.$ $R^2 = 0.005621$ Standard Error (σ) = .02617 F-stat (slopes=0 –i.e., $\beta=0$) = 3.244 (*p-value* = 0.07219) Observations (N) = 576Coefficient P-value Stand Err t-Stat Intercept ($\hat{\alpha}$) -0.00209 0.001157 -1.804 0.0717 $(I_{JAP} - I_{US})(\hat{\beta}) - 0.39148$ 0.217343 -1.801 0.0722 We will test the H₀ (Relative PPP true): $\alpha = 0 \& \beta = 1$ Two tests: (1) *t-tests* (individual tests) (2) F-test (joint test)

Example: Using monthly Japanese and U.S. data (1975: Jan - 2022: Dec), we fit the following regression (Observations = 576): $e_{f,t,T}(\text{JPY/USD}) = (S_t - S_{t-1})/S_{t-1} = \alpha + \beta (I_{IAP} - I_{US})_t + \varepsilon_t.$ $R^2 = 0.005621$ Standard Error (σ) = .02617 F-stat (slopes=0 –i.e., $\beta=0$) = 3.244 (*p-value* = 0.07219) *F-test* (H₀: $\alpha = 0 \& \beta = 1$): 19.185 (*p-value*: < 0.00001) \Rightarrow reject H₀ at 5% level (F_{2.550.05}= 3.012) Coefficient Stand Err t-Stat P-value 0.001157 Intercept ($\hat{\alpha}$) -0.00209 -1.804 0.0717 0.217343 $(I_{IAP} - I_{US})(\hat{\beta})$ -0.39148 -1.801 0.0722 Test H₀, using t-tests ($t_{574.975} = 1.96 - Note$: when N-K > 30, $t_{.975} = 1.96$): $t_{\alpha=0}$: (-0.00209 - 0) $(0.001157) = -1.804 (p-value = .07) \Rightarrow$ cannot reject H₀. $t_{\beta=1}$: (-0.39148 – 1)/(0.217343 = -6.402 (*p*-value: < .00001) \Rightarrow reject H₀.



• PPP: R_t and S_t $\mathbf{R}_{t} = \mathbf{S}_{t} P_{f} / P_{d}$ Recall **R**.: Mussa (1986): **R**_t is more variable under a free float (after 1973). \mathbf{R}_{t} variability is highly correlated with S_{t} variability. Check Second Moments: Volatility (changes in \mathbf{R}_{t}) = 2.706% & Volatility (changes in S_t) = 2.622 (correlation = .983). Almost the same! Exchange Rate: USD/GBP - 1975-2020 Nominal Real 4 2 Real FX Rate 0 8 1990 1980 2000 2010 2020 Date

<u>Implications</u>: Price levels (P_f/P_d) play a very minor role in explaining the movements of **R**_t (prices are **sticky**).

Possible explanations:

(a) Contracts:

Prices cannot be continuously adjusted due to contracts.

(b) Mark-up adjustments:

Manufacturers and retailers moderate increases in their prices in order to keep market share. Changes in S_t are only partially transmitted or *pass-through* to import/export prices.

Average ERPT (exchange rate pass-through) is around **50%** over one quarter and **64%** over the long run for **OECD countries** (for the **U.S., 25%** in the short-run and **40%** over the long run).

(c) Repricing costs (menu costs)

Expensive to adjust continuously prices -a restaurant, re-printing the menu.

(d) Aggregation

Q: Is price rigidity a result of aggregation –i.e., the use of price index? Empirical work using **micro level data** –say, same good (exact UPC!) in Canadian and U.S. grocery stores– show that on average product-level \mathbf{R}_t moves with S_t . But, evidence is not as solid.

• <u>PPP: Puzzle</u>

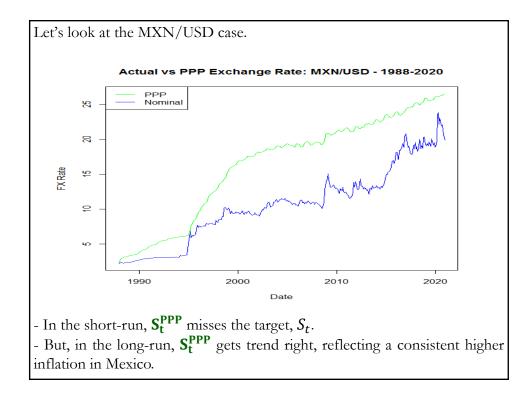
The fact that no single model of exchange rate determination can accommodate both the high persistent of PPP deviations and the high correlation between \mathbf{R}_t and S_t has been called the "**PPP puzzle**."

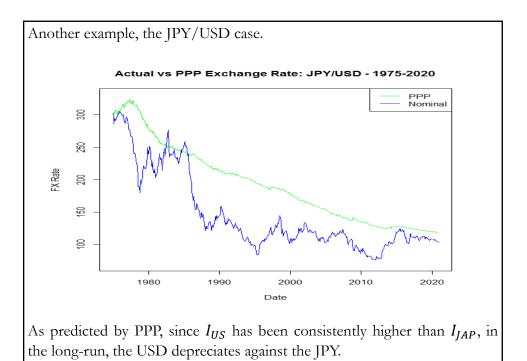
- PPP: Summary of Empirical Evidence
- \mathbf{R}_t and S_t are highly correlated, P_d tends to be sticky.
- In the short run, PPP is a poor model to explain short-term S_t movements.
- PPP deviations are very persistent. They take years to disappear.
- In the long run, there is some evidence of mean reversion, though slow, for \mathbf{R}_t . That is, S_t^{PPP} has long-run information:

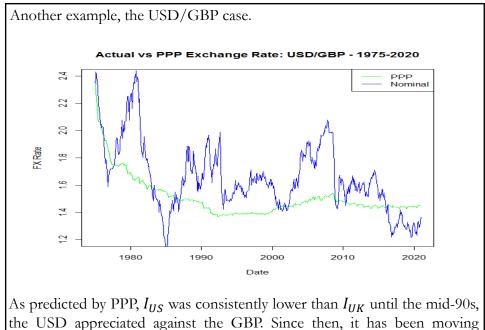
Currencies that consistently have high inflation rate differentials tend to depreciate.

• The long-run interpretation is the one that economists like and use: S_t^{PPP} is seen as a benchmark.

• <u>Calculating S_t^{PPP} (Long-Run FX Rate)</u> We want to calculate $S_t^{PPP} = \frac{P_{d,t}}{P_{f,t}}$ over time. Steps: (1) Divide S_t^{PPP} by $S_{t=0}^{PPP} (=\frac{P_{d,t=0}}{P_{f,t=0}})$ (t = 0 is our starting point). $S_t^{PPP}/S_{t=0}^{PPP} = \frac{P_{d,t}}{P_{f,t}} / (\frac{P_{d,t=0}}{P_{f,t=0}})$ (2) Solve for S_t^{PPP} , after some algebra: $S_t^{PPP} = S_{t=0}^{PPP} * [\frac{P_{d,t}}{P_{d,0}}] * [\frac{P_{f,0}}{P_{f,t}}]$ Assuming $S_{t=0}^{PPP} = S_0 \implies$ we plot $S_t^{PPP} = S_0 * [\frac{P_{d,t}}{P_{d,0}}] * [\frac{P_{f,0}}{P_{f,t}}]$ <u>Note</u>: $S_{t=0}^{PPP} = S_0$ assumes that at t = 0, the economy was in *equilibrium*. This may not be true: Be careful when selecting a base year.







around a constant value.

PPP Summary of Applications:
Equilibrium ("*long-run*") exchange rates.
Explanation of S_t movements.
Indicator of competitiveness or under/over-valuation.
International GDP comparisons: Instead of using S_t, S^{PPP}_t is used to translate local currencies to USD.
Example: Chinese GDP per capita – Nominal & PPP in USD Nominal GDP per capita: CNY 98,404.03 S_t = 0.1391 USD/CNY; S^{PPP}_t = 0.2944 USD/CNY (= P_{d=US}/P_{f=Ch})
R_t = S_t/S^{PPP}_t = 0.1391/0.2944 = 0.4725 ⇒ "goods in the U.S. are 52.75% more expensive than in China."
Nominal GDP (USD) = CNY 98,404.03 * 0.1391 USD/CNY = USD 13,688
PPP GDP (USD) = CNY 98,404.03 * 0.2944 USD/CNY = USD 28,978.

	GDP per capita (in USD) - 2025		
Country	Nominal	PPP	
Luxembourg	140,941	152,915	
USA	89,105	89,105	
Japan	33,956	54,677	
Italy	41,091	63,076	
Czech Republic	33,039	59,368	
Costa Rica	19,095	31,463	
Brazil	9,964	23,239	
China	13,688	28,978	
Vietnam	4,806	17,612	
Algeria	5,691	18,525	
India	2,878	12,132	
Ethiopia	1,066	4,398	
Mozambique	663	1,729	
l <u>ote</u> : PPP GDP/Nominal GD ⇒ "One USD has 11			